















$$W = N \cos \beta + \frac{W}{12} (12 \sin^2 \beta + \cos \beta)$$

$$N = \frac{W}{12 \cos \beta} (-12 \sin^2 \beta + \cos \beta + \frac{5}{12} \sin 2\beta)$$

$$= \frac{W}{2 \cos \beta} (\cos \beta - 12 \sin^2 \beta + \frac{5}{12} \sin 2\beta)$$

$$N = \frac{W}{2} (1 + \cos 2\beta + \frac{5}{12} \sin 2\beta)$$

Mass of hemisphere = $\frac{2}{3} \pi a^3$
 Mass of strip = $\pi x^2 \delta y$
 C of G of strip about base at y = $\frac{3}{4} x^2$

∴ Taking moments about base

$$\frac{2}{3} \pi a^3 \bar{y} = \pi \int_0^a x^2 y dy$$

$$\text{Since } x^2 = a^2 - y^2 \quad \frac{2a^2 \bar{y}}{3} = \int_0^a (a^2 - y^2) y dy$$

$$\frac{2a^2 \bar{y}}{3} = \left[\frac{a^2 y^2}{2} - \frac{y^4}{4} \right]_0^a$$

$$\therefore \bar{y} = \frac{3a}{8} \quad \text{ie Cent of mass at } \frac{3a}{8} \text{ from base.}$$



$$\text{Mass of cone} = \frac{1}{3} \pi a^3$$

$$\therefore \text{Total wt. of toy} = W$$

$$\therefore \text{wt of cone} = \frac{W}{3} \quad \text{wt. of hemisphere} = \frac{2W}{3}$$

C of Mass of cone at dist. $\frac{a}{4}$ from its plane base

∴ Taking moments about vertex of cone

$$W \bar{y} = \frac{W}{3} \left(a + \frac{3a}{8} \right)$$

$$\bar{y} = \frac{a}{6} + \frac{1}{4} a$$

$$\bar{y} = \frac{7a}{6} \quad \text{ie Cent of mass at } \frac{7a}{6} \text{ from vertex.}$$

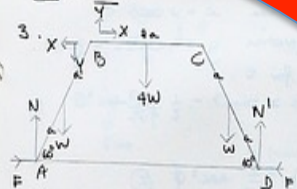


Since N ⊥ to horiz plane, the Cent of plane (base of hemisphere) N acts

∴ Taking moments about Cent of plane

$$\frac{W a \cos \theta}{6} = C \quad \text{ie Couple of magnitude } \frac{W a \cos \theta}{6}$$

1962. A. 36.



Taking moments about B for AB

$$2a \cdot \frac{\sqrt{3}}{2} F + \frac{W a}{2} = \frac{2a N}{2}$$

$$2\sqrt{3} F + W = 2N$$

$$F = \frac{2N - W}{2\sqrt{3}}$$

Taking moments about A for AC

$$\frac{W a}{2} = X \cdot \frac{2a \sqrt{3}}{2} - Y \cdot \frac{2a}{2}$$

$$Y = -\frac{W}{2} + \sqrt{3} X$$

Taking moments about C for BC

$$= 2a Y$$

$$= 2a \left(-\frac{W}{2} + \sqrt{3} X \right)$$

$$= 2a Y$$

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By symmetry

$$6W$$

$$= N'$$

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Quicker to res for AB

parallel







